

# Propagation and focusing of modes of the dielectric resonator of terahertz laser

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**Abstract**— Theoretically on the basis of the vectorial Rayleigh-Sommerfeld theory and experimentally using terahertz radiation of the waveguide laser ( $\lambda = 0.4326$  mm) the physical features of propagation and "moderate" or "sharp" focusing of laser beams of radiation are investigated in free space which described by modes of circular hollow dielectric waveguide with different spatial polarization.

**Keywords**— propagation; focusing; terahertz laser; dielectric resonator, modes.

The purpose of this work is to study features of the structure of the field of waveguide modes for the dielectric resonator of the terahertz laser in the near- and far-field of diffraction and their focusing for various types of spatial polarization of these modes.

## I. THEORETICAL RELATIONSHIPS

Let us assume radiation is given in the initial plane in the form of symmetric azimuthally, radially and linearly polarized  $TE_{01}$ ,  $TM_{01}$ ,  $EH_{11}$  modes and asymmetrical linearly polarized  $TE_{01} + EH_{21}$  mode of circular dielectric waveguide. Components of electromagnetic fields for these modes have well-known form. We described the components of the vector of electric field using the Rayleigh-Sommerfeld integrals and obtained the expressions for the transverse and longitudinal components of the field in the free space in different zones of diffraction and in the focal plane of the lens.

## II. RESULTS AND THEIR DISCUSSION

The wavelength of radiation was selected in the middle part of terahertz range  $\lambda = 0.4326$  mm (generation line of laser with optical pumping on molecule  $CH_3OH$ ). For comparison of spatial characteristics of the studied modes and modes of free space it was analyze the propagation in free space linearly polarized axially symmetric Gaussian beam with a radius equal to the radius of waveguide  $EH_{11}$  mode at the  $e^{-2}$  level of its maximum value at the output end of the waveguide.

The transverse intensity distributions of the components of the electric field vector and the total field intensity of radiation beams were studied for the investigated waveguide modes in the field of minimum size of the focused beam. Focal length of the lens is selected suitably conditions of "moderate" (numerical aperture  $NA \leq 0.7$ ) and "sharp" ( $NA \sim 1$ ) focusing.

## III. CONCLUSIONS

We have established that the stable structure of the field is observed for  $TE_{01}$ ,  $TM_{01}$ ,  $EH_{11}$  and  $TE_{01} + EH_{21}$  modes in the terahertz range at shorter distances from the end of waveguide ( $L \geq 2a^2/\lambda$ ) in contrast to the distances predicted by known Rayleigh criterion ( $L \geq 8a^2/\lambda$ ) for far-field zone of diffraction.

Numerical simulations show that in the case of "moderate" and "sharp" focusing for the intensity of the components of a vector of an electric field and the total field in the focus of the lens the following physical features are observed:

- the transverse  $E_x$ -component of the field has a maximum value of the intensity for  $TE_{01}$  and  $TM_{01}$  modes;
  - the maximum intensity value for the transverse  $E_y$  component of field is observed for the  $EH_{11}$  mode and the minimum value is for the  $TE_{01}$  and  $TM_{01}$  modes;
  - the longitudinal  $E_z$  component of a field has its maximum value of intensity for  $TM_{01}$  mode. However, if the  $NA \leq 0.7$ , its value is less than 4 %, then the  $NA \sim 1$ , it increases to 40 % from the corresponding values for the transverse components. Significant growth of this component is also observed for  $EH_{11}$  mode – from 0.2 % at  $NA \leq 0.7$  to 6 % at  $NA \sim 1$ ;
  - the transverse intensity distribution of the longitudinal  $E_z$  component of a field for  $TM_{01}$  mode has the form of the sampling function but for  $EH_{11}$  mode it has annular character. The annular intensity distribution is observed for all components of the field for  $TE_{01}$  mode;
  - the maximum value of the total radiation intensity is observed for  $EH_{11}$  mode and the minimum value for  $TE_{01}$  and  $TM_{01}$  modes;
  - the diameter of the focused spot for  $EH_{11}$  mode is 1.5 times smaller than the diameter of the focused spot for other modes.
- Experimental studies confirmed the conclusion that the maximum value of the total radiation intensity and the minimum diameter of the focused spot is observed for  $EH_{11}$  mode.